

**Sample Paper**  
**10+2**  
**Mathematics (For DA Students)**

**Time : 3 Hours**

**Maximum Marks : 80**

**Instructions:**

1. Section A contains Q1 to Q26 (objective type questions) of 2 marks each.
2. Section B contains Q27 to Q34 of 3 marks each.
3. Section C contains Q35 to Q42 of 4 marks each.
4. All questions of Section A are compulsory. Attempt any 4 questions out of 8 questions in Section B. Attempt any 4 questions out of 8 questions in Section C.

**Section A**

**Choose a correct option from the given options from Q1 to Q7 :**

- Q1 Let  $R = \{(a, b) : a = b - 2, b > 6\}$  be a relation defined on the set  $\mathbb{N}$  of natural numbers, then 2  
(a)  $(2, 4) \in R$  (b)  $(3, 8) \in R$  (c)  $(6, 8) \in R$  (d)  $(8, 7) \in R$
- Q2 The function  $f: \mathbb{R} \rightarrow \mathbb{R}$  given by  $f(x) = 2x - 5$  is 2  
(a) one-one only (b) onto only (c) one-one and onto (d) not onto
- Q3 Principal value of  $\sin^{-1}\left(\frac{-1}{2}\right)$  is 2  
(a)  $-\frac{\pi}{6}$  (b)  $\frac{\pi}{6}$  (c)  $-\frac{\pi}{3}$  (d)  $\frac{\pi}{3}$
- Q4 If  $y = \sin^{-1}(x)$  then  $x$  belongs to the interval : 2  
(a)  $(0, \pi)$  (b)  $(-1, 1)$  (c)  $[-1, 1]$  (d)  $[0, \pi]$
- Q5 If order of matrix  $A$  is  $2 \times 3$  and order of matrix  $B$  is  $3 \times 5$  then order of matrix  $B'A'$  is : 2  
(a)  $5 \times 2$  (b)  $2 \times 5$  (c)  $5 \times 3$  (d)  $3 \times 2$
- Q6 If  $\begin{vmatrix} x & 1 \\ 1 & x \end{vmatrix} = \begin{vmatrix} 2 & 0 \\ 8 & 4 \end{vmatrix}$  then value of  $x$  is : 2  
(a)  $\pm 3$  (b)  $\pm 2$  (c)  $\pm 4$  (d)  $\pm 8$
- Q7 If  $\begin{bmatrix} 2x+y & 0 \\ 5 & x \end{bmatrix} = \begin{bmatrix} 5 & 0 \\ 5 & 3 \end{bmatrix}$ , then  $y$  is equal to:- 2  
(a) 1 (b) 3 (c) 2 (d) -1

**Match the columns from Q8 to Q13 :**

- |     |   |   |   |
|-----|---|---|---|
| Q8  | <b>Col. A</b><br>(a) $A + A'$<br>(b) $A - A'$                                 | <b>Col. B</b><br>(i) Always a null Matrix<br>(ii) Symmetric Matrix<br>(iii) Skew-Symmetric Matrix                           | 2 |
| Q9  | <b>Col. A</b><br>(a) $f(x) = e^x$<br>(b) $f(x) = \frac{1}{x}$                 | <b>Col. B</b><br>(i) Continuous function<br>(ii) Identity function<br>(iii) Discontinuous function                          | 2 |
| Q10 | <b>Col. A</b><br>(a) $\frac{d}{dx}(\sin x)$<br><br>(b) $\frac{d}{dx}(\cos x)$ | <b>Col. B</b><br>(i) $\tan x$<br><br>(ii) $\cos x$<br>(iii) $-\sin x$   | 2 |
| Q11 | <b>Col. A</b><br>(a) $f(x) = -x$<br>(b) $f(x) = e^x$                          | <b>Col. B</b><br>(i) Strictly increasing function<br>(ii) Strictly decreasing function<br>(iii) Constant function           | 2 |
| Q12 | <b>Col. A</b><br>(a) $f''(a) < 0$<br>(b) $f''(a) > 0$                         | <b>Col. B</b><br>(i) $x = a$ is point of minima<br>(ii) $x = a$ is point of maxima<br>(iii) $x = a$ is a point of inflexion | 2 |
| Q13 | <b>Col. A</b><br>(a) $\int dx$<br>(b) $\int \cos x \, dx$                     | <b>Col. B</b><br>(i) $-\sin x + c$<br>(ii) $x + c$<br>(iii) $\sin x + c$  | 2 |

Fill in the blanks from Q14 to Q20 from the the following options :

$$\left\{ -2, \sqrt{426}, \frac{1}{2}, \int_1^4 x^2 dx, 4 \int_0^3 \sqrt{9-x^2} dx, 2, e^{2x}, 5, \tan x \right\}$$

- Q14  $\int_0^1 x dx =$  \_\_\_\_\_ 2
- Q15 Area of the region bounded between parabola  $y = x^2$  and lines  $x = 1, x = 4$  in the first quadrant is given by the integral \_\_\_\_\_ 2
- Q16 Area of the circle  $x^2 + y^2 = 9$  is given by the integral \_\_\_\_\_ 2
- Q17 Order of the differential equation  $\frac{d^2 y}{dx^2} + \left(\frac{dy}{dx}\right)^3 + y = 0$  is \_\_\_\_\_ 2
- Q18 Integrating factor of the differential equation  $\frac{dy}{dx} + 2y = \cos x$  is \_\_\_\_\_ 2
- Q19 If  $\vec{a} = \hat{i} - 2\hat{j} + \hat{k}$  and  $\vec{b} = 3\hat{i} + 2\hat{j} - \hat{k}$  then  $\vec{a} \cdot \vec{b} =$  \_\_\_\_\_ 2
- Q20 If  $\vec{a} = \hat{i} + \hat{j} + \hat{k}$  and  $\vec{b} = \hat{i} + 2\hat{j} + 3\hat{k}$  then  $|\vec{a} \times \vec{b}| =$  \_\_\_\_\_ 2

State as True or False from Q21 to Q26.

- Q21 Direction ratios of  $x$  -axis are  $\langle 0, 1, 1 \rangle$ . 2
- Q22  $\frac{x-2}{3} = \frac{y+7}{2} = \frac{z-9}{5}$  is the vector form of equation of line. 2
- Q23 Subject to the constraints  $x + y \leq 3, x \geq 0, y \geq 0$  maximum value of  $Z = 2x + y$  is 6. 2
- Q24 Subject to the constraints  $x + y \leq 5, x \geq 0, y \geq 0$  maximum value of  $Z = x + 2y$  is 5. 2
- Q25 If  $P(A) = 0.3$  then  $P(\bar{A}) = 0.6$ . 2
- Q26 If  $P(A) = 0.5, P(A \cap B) = 0.2$  then  $P(B / A) = 0.4$  2

### Section B

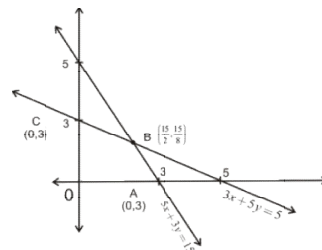
This section contains 8 questions of 3 marks each. Attempt any 4 questions out of these questions .

- Q27 Find the value of  $4 \tan^{-1}(1) - \cos^{-1}\left(-\frac{1}{2}\right)$  3
- Q28 Form a matrix  $A = [a_{ij}]$  of order  $2 \times 2$  where  $a_{ij} = i + j$ . 3
- Q29 If  $y = \cos 2x - \sin 5x$  then find  $\frac{dy}{dx}$ . 3
- Q30 Evaluate  $\int_0^1 \frac{dx}{1+x^2}$ . 3
- Q31 Find the area of the region bounded by the parabola  $y^2 = x$  lines  $x = 0, x = 3$  and  $x$  - axis in the first quadrant. 3
- Q32 If  $\vec{a} = 3\hat{i} - \hat{j} + \hat{k}$  and  $\vec{b} = 5\hat{i} + \hat{j} - 7\hat{k}$  then find  $|\vec{a} \times \vec{b}|$ . 3
- Q33 Find the vector and Cartesian equation of the line which passes through the points  $(3, -2, -4)$  and  $(5, -7, 8)$ . 3
- Q34 If  $P(A) = \frac{6}{11}, P(B) = \frac{5}{11}$  and  $P(A \cup B) = \frac{7}{11}$  then find  $P(A \cap B)$ . 3

### Section C

This section contains 8 questions of 4 marks each. Attempt any 4 questions out of these questions .

- Q35 Give two examples each of : (i) row matrix 4  
(ii) square matrix
- Q36 Write the formula of differentiation using : 4  
(i) Product Rule (ii) Quotient Rule
- Q37 Give one example each of an increasing function and a decreasing function. 4
- Q38 Find the area bounded by ellipse  $\frac{x^2}{9} + \frac{y^2}{16} = 1$  4
- Q39 Formulate the integral to find the area bounded by the circle  $x^2 + y^2 = 25$  in the first quadrant. 4
- Q40 Give one example each of (i) Homogenous differential equation 4  
(ii) First order linear differential equation
- Q41 Shade the feasible region in the given figure 4  
subject to the constraints  
 $5x + 3y \leq 15, 3x + 5y \leq 15, x \geq 0, y \geq 0$ .  
Also maximize  $Z = 8x + 16y$  for this graph.



- Q42 Two balls are drawn at random with replacement from a box containing 10 black balls and 8 red balls. Find the probability that one of them is black and other is red. 4